

GCSE

Applications of Mathematics (Pilot)

Unit **A381/02**: Higher Tier

General Certificate of Secondary Education

Mark Scheme for June 2016

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations used in the detailed Mark Scheme.

Annotation	Meaning
✓	Correct
✗	Incorrect
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working (after correct answer obtained), provided method has been completed
M0	Method mark awarded 0
M1	Method mark awarded 1
M2	Method mark awarded 2
A1	Accuracy mark awarded 1
B1	Independent mark awarded 1
B2	Independent mark awarded 2
MR	Misread
SC	Special case
^	Omission sign

These should be used whenever appropriate during your marking.

The **M**, **A**, **B**, etc annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks.

It is vital that you annotate these scripts to show how the marks have been awarded.

It is not mandatory to use annotations for any other marking, though you may wish to use them in some circumstances.

Subject-Specific Marking Instructions

- M** marks are for using a correct method and are not lost for purely numerical errors.
A marks are for an accurate answer and depend on preceding **M** (method) marks. Therefore **M0 A1** cannot be awarded.
B marks are independent of **M** (method) marks and are for a correct final answer, a partially correct answer, or a correct intermediate stage.
SC marks are for special cases that are worthy of some credit.
- Unless the answer and marks columns of the mark scheme specify **M** and **A** marks etc, or the mark scheme is 'banded', then if the correct answer is clearly given and is not from wrong working **full marks** should be awarded.

Do not award the marks if the answer was obtained from an incorrect method, ie incorrect working is seen and the correct answer clearly follows from it.

3. Where follow through (**FT**) is indicated in the mark scheme, marks can be awarded where the candidate's work follows correctly from a previous answer whether or not it was correct.

Figures or expressions that are being followed through are sometimes encompassed by single quotation marks after the word *their* for clarity, eg FT $180 \times (\textit{their} '37' + 16)$, or FT $300 - \sqrt{(\textit{their} '5^2 + 7^2')}$. Answers to part questions which are being followed through are indicated by eg FT 3 $\times \textit{their} (a)$.

For questions with FT available you must ensure that you refer back to the relevant previous answer. You may find it easier to mark these questions candidate by candidate rather than question by question.

4. Where dependent (**dep**) marks are indicated in the mark scheme, you must check that the candidate has met all the criteria specified for the mark to be awarded.

5. The following abbreviations are commonly found in GCSE Mathematics mark schemes.

- **figs 237**, for example, means any answer with only these digits. You should ignore leading or trailing zeros and any decimal point eg 237000, 2.37, 2.370, 0.00237 would be acceptable but 23070 or 2374 would not.
- **isw** means **ignore subsequent working** after correct answer obtained and applies as a default.
- **nfw** means **not from wrong working**.
- **oe** means **or equivalent**.
- **rot** means **rounded or truncated**.
- **seen** means that you should award the mark if that number/expression is seen anywhere in the answer space, including the answer line, even if it is not in the method leading to the final answer.
- **soi** means **seen or implied**.

6. In questions with no final answer line, make no deductions for wrong work after an acceptable answer (ie **isw**) unless the mark scheme says otherwise, indicated by the instruction 'mark final answer'.

7. In questions with a final answer line following working space,

(i) if the correct answer is seen in the body of working and the answer given on the answer line is a clear transcription error allow full marks unless the mark scheme says 'mark final answer'. Place the annotation ✓ next to the correct answer.

- (ii) if the correct answer is seen in the body of working but the answer line is blank, allow full marks. Place the annotation ✓ next to the correct answer.
- (iii) if the correct answer is seen in the body of working but a completely different answer is seen on the answer line, then accuracy marks for the answer are lost. Method marks could still be awarded. Use the M0, M1, M2 annotations as appropriate and place the annotation ✕ next to the wrong answer.
8. In questions with a final answer line:
- (i) If one answer is provided on the answer line, mark the method that leads to that answer.
- (ii) If more than one answer is provided on the answer line and there is a single method provided, award method marks only.
- (iii) If more than one answer is provided on the answer line and there is more than one method provided, award zero marks for the question unless the candidate has clearly indicated which method is to be marked.
9. In questions with no final answer line:
- (i) If a single response is provided, mark as usual.
- (ii) If more than one response is provided, award zero marks for the question unless the candidate has clearly indicated which response is to be marked.
10. When the data of a question is consistently misread in such a way as not to alter the nature or difficulty of the question, please follow the candidate's work and allow follow through for **A** and **B** marks. Deduct 1 mark from any **A** or **B** marks earned and record this by using the MR annotation. **M** marks are not deducted for misreads.
11. Unless the question asks for an answer to a specific degree of accuracy, always mark at the greatest number of significant figures even if this is rounded or truncated on the answer line. For example, an answer in the mark scheme is 15.75, which is seen in the working. The candidate then rounds or truncates this to 15.8, 15 or 16 on the answer line. Allow full marks for the 15.75.
12. Ranges of answers given in the mark scheme are always inclusive.
13. For methods not provided for in the mark scheme give as far as possible equivalent marks for equivalent work. If in doubt, consult your Team Leader.
14. Anything in the mark scheme which is in square brackets [...] is not required for the mark to be earned, but if present it must be correct.

MARK SCHEME

Question		Answer	Marks	Part marks and guidance	
1	(a)	$60 \div 200 = 0.3$ Or $200 \times 0.3 = 60$ Or $60 \div 0.3 = 200$	1		
	(b)*	44 times supported by clear working: $105 \div 2.4 = 43.75$	3	2 for $(60 + 45) \div 2.4$ oe or 44 with incomplete working or 43.75 supported by correct working or 43 with incomplete or inaccurate working Or 1 for 2.4 clearly identified as common multiple or $(60 + 45) \div$ figs 24 or better, may be implied by first 4 or 5 multiples of 24 followed by answer of 4 or 5 or $(1.75 \div \text{figs } 24) \times 60$ or 437 given as final answer	$(1.75 \div 2.4) \times 60$ Condone (for clear working) listing multiples of 0.3 and 0.8 For clearly identified as a minimum must see lists of multiples for both 0.3 & 0.8 & at least one stops at 2.4 or 2.4 circled in both Do not award 1 for just answer of 4 or 5 without working
2	(a)	[Iron:] 61 to 62 and [Zirconium:] 81 to 82 nfw Zirconium Or <i>their</i> choice of harder metal FT <i>their</i> calculated figures seen & clearly related to the metals	3 And 1	B2 for 61 to 62 or 81 to 82 nfw Or B1 for $\frac{1.85 \times 100}{1.73^2}$ and $\frac{1.85 \times 150}{1.84^2}$ or 185 or 2.9929 or 277.5 .. or 3.3(856 ...) seen If B0 then SC1 for 33... and 44... Or 106 to 107 and 150 to 151	Both values nfw Allow Iron is the softer metal Zirconium with no working scores 0

Question		Answer	Marks	Part marks and guidance	
	(b)	49 to 49.2	4	<p>B3 for $[Z =]$ 10.16 to 10.2</p> <p>Or</p> <p>B2 for $[W =]$ 0.64 to 0.65</p> <p>Or</p> <p>M1 for 87.4 to 87.5 or 9.3 to 9.4 or $10 - \sqrt{10^2 - 3.54^2}$ oe seen</p> <p>If B2 or M1 then also</p> <p>M1 for $1.57 \times 10 \times \textit{their } 0.647 \dots$ or $500 \div \textit{their } Z (10.1664\dots)$ seen</p> <p>If 0 scored then</p> <p>SC3 for $\frac{500}{1.57 \times 10 \times (10 - \sqrt{10^2 - 3.54^2})}$</p> <p>Or</p> <p>SC2 for $\frac{P}{1.57 \times D \times (D - \sqrt{D^2 - d^2})}$</p>	<p>Answer 49 to 49.2 with no working shown scores full marks</p> <p><i>Their Z</i> could be, as an example: $(Z=)$ $1.57 + \textit{their } D + \textit{their } W$ but would still gain for $500 \div \textit{their } W$</p>
3	(a)	0.988449 cao	2	<p>B1 for any of 209.3 or 159.56 or 281 or 44836.36 or 211.7... or 0.988...</p>	

Question		Answer	Marks	Part marks and guidance																																	
	(b)	Single ruled line, passing through (10, 8.8) and (60, 74.3) correct to within ½ small square	2	M1 for 1 correct point plotted or calculated or correct part line or line with correct gradient	If single correct line ignore extra incorrect points & award 2 marks If more than one line M1 max for correct points Points may include: <table border="1" style="display: inline-table; margin: 5px;"> <thead> <tr> <th>x</th> <th>y</th> <th>x</th> <th>y</th> </tr> </thead> <tbody> <tr> <td>5</td> <td>2.3</td> <td>40</td> <td>48.1</td> </tr> <tr> <td>10</td> <td>8.8</td> <td>45</td> <td>54.7</td> </tr> <tr> <td>15</td> <td>15.4</td> <td>50</td> <td>61.2</td> </tr> <tr> <td>20</td> <td>21.9</td> <td>55</td> <td>67.8</td> </tr> <tr> <td>25</td> <td>28.5</td> <td>60</td> <td>74.3</td> </tr> <tr> <td>30</td> <td>35</td> <td>65</td> <td>80.9</td> </tr> <tr> <td>35</td> <td>41.6</td> <td>70</td> <td>87.4</td> </tr> </tbody> </table>	x	y	x	y	5	2.3	40	48.1	10	8.8	45	54.7	15	15.4	50	61.2	20	21.9	55	67.8	25	28.5	60	74.3	30	35	65	80.9	35	41.6	70	87.4
x	y	x	y																																		
5	2.3	40	48.1																																		
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15	15.4	50	61.2																																		
20	21.9	55	67.8																																		
25	28.5	60	74.3																																		
30	35	65	80.9																																		
35	41.6	70	87.4																																		
4	(a)*	Correct appropriate calculation(s) with solution(s) to 4 sig figs or better linked to clear explanation with reference to rounding as appropriate Eg 38% of 2340 = 889.2 which can be rounded to 890 Eg $(890/2340) \times 100 = 38.03\%$ which rounds to 38% Eg $(890 \div 38) \times 100 = 2342$ so one of the numbers must be rounded Eg $(890/2340) \times 100 = 38.03\% \approx 38\%$	3	2 for correct calculation(s) with solution to accuracy below or better Eg 38% of 2340 = 889.2 Eg $(890/2340) \times 100 = 38.03\% = 38\%$ Eg $890 \div 38 = 23.4[2..]$ & $23.4[2..] \times 100 = 2340$ Or 1 for one correct calculation shown Eg $2340 \times 38\% = 889$ or $=890$ Eg $(890/2340) \times 100 = 38\%$ Eg $890/2340 = 0.38...$ Eg $890 \div 38 = 23.4[2..]$	For all 3 marks explanation must mention rounding or approximately oe Accept clear \approx for their explanation Accept alternatives with clear explanations Eg $0.38 \times 2340 = 889.2$ & $0.381 \times 2340 = 891.5$ so 38% must be rounded Do not accept 'so it's the same' for an explanation If correct & incorrect calculations assume contradictory unless explanation clearly follows from one																																

Question		Answer	Marks	Part marks and guidance		
	(b)	1080 Or 1078, 1079, or 1081 with correct supporting working	4	<p>M2 for $1 - \left(\frac{2}{5} + \frac{1}{6}\right)$ oe soi by $\frac{13}{30}$</p> <p>Or</p> <p>M1 for $\frac{2}{5} + \frac{1}{6}$ oe soi by $\frac{17}{30}$</p> <p>And</p> <p>M1 for $468 \div \textit{their} \frac{13}{30}$ or $468 \div \textit{their} \frac{17}{30}$ or $468 \times \textit{their} \frac{30}{13}$ or $468 \times \textit{their} \frac{30}{17}$</p> <p>If M0 then SC1 for $468 \div 8/11$ oe or $468 \div 3/11$</p>	<p>For method marks follow their working, may be seen embedded or in stages</p> <p>Allow working with equivalent fractions or decimal or % rot to 2 sig figs or better, ie</p> <p>M2 for $1 - (0.4 + 0.16 \text{ to } 0.17)$ soi by 0.43 to 0.44</p> <p>Or</p> <p>M1 for $0.4 + 0.16 \text{ to } 0.17$ soi by 0.56 to 0.57</p> <p>And</p> <p>M1 for $468 \div \textit{their} 0.43$ oe or $468 \div \textit{their} 0.57$ <i>their</i> 13/30 or 17/30 must come from attempt at adding fractions 2/5 and 1/6 seen 643 to 644 1716</p>	
	(c)	(i)	87.5	2	<p>M1 for figs $175 \div 0.2$ oe</p> <p>If M0 allow SC1 for figs 875</p>	<p>figs 175×5 May be done in stages Allow full marks for 87 500 000 if "million" crossed out.</p>
		(ii)	51.49 or 51.5	2	<p>M1 for figs 38×1.355 oe</p> <p>If M0 allow SC1 for figs 5149 or figs 515 or 13.49 or 13.5 seen</p>	<p>May be done in stages Condone full marks for 51 490 000 or 51 500 000 without 'million' crossed out if penalised in part (c)(ii)</p>
		(iii)	41.5 Allow 42 supported by correct method shown	2	<p>M1 for $(99.9 - 70.6) \div 70.6$ oe or $(99.9 \div 70.6)$ oe</p>	<p>$29.3 \div 70.6$</p>

Question		Answer	Marks	Part marks and guidance	
	(iv)	1.4[2][%] decrease	4	<p>M3 for $[1 -](1.06 \times 0.93)$ oe</p> <p>Or</p> <p>M2 for 1.06 and 0.93 oe soi</p> <p>Or</p> <p>M1 for 1.06 or 0.93 oe soi</p> <p>If M0 then SC1 for 106 or 93</p>	<p>0.9858 or 98.58 or 98.6 or 0.014[2]</p> <p>M2 can be implied by 9858</p> <p>Follow through all method marks where values given as percentages 106% or 93%</p> <p>If using assumed value for 2012 follow method & award M marks as appropriate where working seen</p>
	(d)	$600t + 210\frac{t}{2} = 33840$ oe 48	1 And 2	<p>M1 for $[t =] 33840 \div (600 + 210/2)$ or better</p> <p>If 0 and M0 then SC1 for $600t + 210\frac{t}{2}$ oe seen</p>	<p>$705t = 33840$ Condone inclusion of £ sign</p>
	(e)	<p>$x + 10$ and $3x$ seen or implied by correct equation or answer of 18</p> <p>$26 + (x + 10) + (180 - 3x) = 180$ oe</p> <p>18</p>	1 And 2 And 1	<p>M1 for using sum angles in triangle correctly to form an equation in x for <i>their</i> angles PQB and PRQ, must follow from diagram</p>	<p>Allow $3 \times x$ for $3x$ May be seen on diagram, in correct or incorrect place, or in working</p> <p>$3x = x + 10 + 26$ or better</p> <p>18 with no or incorrect working scores 2 marks</p>

Question		Answer	Marks	Part marks and guidance	
5	(a)	38.5 Or 39 from correct working	3	M2 for $46.2 \times \frac{40}{48}$ or $46.2 \div \frac{48}{40}$ oe Or M1 for [h/40 =] 46.2/48 or [h/46.2 =] 40/48	$40 \div 48 = \frac{5}{6}$ or 0.83[33...] $48 \div 40 = 1.2$ $46.2 \div 48 = 0.9625$
	(b)	66.39 to 66.4 Or awrt 66 provided full correct method shown	4	M3 for $58 \times \sqrt[3]{\frac{7.5}{5}}$ oe Or M2 for $\sqrt[3]{\frac{7.5}{5}}$ soi by 1.14 to 1.15 oe Or M1 for 1.5 or $0.\dot{6}$ or $\sqrt[3]{7.5}$ or $\sqrt[3]{5}$ seen If M0 then SC1 for final answer 87	$58 \div \sqrt[3]{0.\dot{6}}$ May be done in stages $\sqrt[3]{0.\dot{6}} = 0.87$ to 0.88 1.957 to 1.96 or 1.7099... to 1.71 for $0.\dot{6}$ allow 0.66 to 0.67
	(c)	(£)2925	4	M2 for $L = (1 + \frac{2}{3})S$ oe And $S + 2L = 2S + L + 1950$ oe Or M1 for $L = (1 + \frac{2}{3})S$ oe or $S + 2L = 2S + L + 1950$ oe And M1 for $S + \frac{10}{3}S = 2S + \frac{5}{3}S + 1950$ oe Or $\frac{3}{5}L + 2L = \frac{6}{5}L + L + 1950$ oe If first M1 then also SC1 for correctly combining their two equations for a single variable	Allow M marks for using decimal equivalents with at least 3 decimal places, rot. For M1 if not L and S their equations must follow their defined variables if given Award M3 for $\frac{2}{3}S = 1950$ or $1950 \div \frac{2}{3}$ oe or $\frac{2}{5}L = 1950$

Question		Answer	Marks	Part marks and guidance	
	(d)	(i)	[0]32	2	M1 for 212 – 180 oe seen 180 – (360 – 212)
		(ii)	Point marked correctly (use overlay)	3	M1 for line drawn at bearing of 312 to 314° at Jinan's crane And M1 for line drawn at bearing of 30 to 32° at Heather's crane. May not be labelled "Carmella's crane", but must be unambiguous for full marks Full marks may be awarded for correct positioning but with missing or incomplete construction lines.

Question	Answer	Marks	Part marks and guidance
6	$\frac{29}{98}$ or an equivalent proper fraction Or 0.2959 to 0.296 if given as a decimal	4	<p>Using AC & BC consistently in correct proportions as integers, fractions, decimals, decimals to 2dp rot or better</p> <p>Using AB as 2, BC as 5:</p> <p>M2 for area one or both white triangles</p> <p>Or M1 for area one or two or four grey triangles</p> <p>And M1 for area white triangle ÷ area large square oe</p> <p><u>Alternative approach using Pythagoras:</u> M3 for $\frac{1}{2} \times \left(\left(\frac{2}{7} \right)^2 + \left(\frac{5}{7} \right)^2 \right) [= \frac{1}{2} \times \left(\frac{\sqrt{29}}{7} \right)^2]$ oe or $\frac{\frac{1}{2} \times (2^2 + 5^2)}{7 \times 7} [= \frac{14.5}{49}]$ oe</p> <p>Or M2 for $\sqrt{\left(\frac{2}{7} \right)^2 + \left(\frac{5}{7} \right)^2} [= \frac{\sqrt{29}}{7}]$ oe or $\frac{1}{2} \times (2^2 + 5^2) [= 14.5]$ oe</p> <p>Or M1 for $\left(\left(\frac{2}{7} \right)^2 + \left(\frac{5}{7} \right)^2 \right) [= \frac{29}{49}]$ oe or $\sqrt{2^2 + 5^2}$ oe</p> <p>M marks may be embedded & may be done in stages</p> <p>Possibilities include:</p> <p>One white triangle: $\frac{1}{2} (49 - 4 \times 5) [= 14.5]$ oe $\frac{1}{2} \times \left(1 - 4 \times \frac{1}{2} \times \left(\frac{2}{7} \times \frac{5}{7} \right) \right)$ oe</p> <p>One Grey triangle: $0.5 \times 2 \times 5 [= 5]$ Or $\frac{1}{2} \times \left(\frac{2}{7} \times \frac{5}{7} \right) [= \frac{5}{49}]$ oe</p> <p>nb M3 for $\frac{1}{2} \times \left(1 - 4 \times \frac{1}{2} \times \left(\frac{2}{7} \times \frac{5}{7} \right) \right)$ or $\frac{\frac{1}{2} \times (7 \times 7 - 4 \times \frac{1}{2} \times (2 \times 5))}{7 \times 7}$ or $\frac{(\frac{1}{2} \times 7 \times 7 - 2 \times \frac{1}{2} \times (2 \times 5))}{7 \times 7}$</p> <p>For misread must indicate lengths clearly on diagram or in working, most obvious is AB is 2/7 of BC, follow their calculations for area triangles etc & award M marks as appropriate</p> <p>$2/7 = 0.2857... \quad 5/7 = 0.714...$</p>

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