

# ADVANCED SUBSIDIARY GCE MATHEMATICS

Probability & Statistics 1

4732

Candidates answer on the Answer Booklet

#### **OCR Supplied Materials:**

- 8 page Answer Booklet
- List of Formulae (MF1)

#### **Other Materials Required:**

None

Monday 15 June 2009 Afternoon

Duration: 1 hour 30 minutes



#### **INSTRUCTIONS TO CANDIDATES**

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Answer Booklet.
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.
- You are permitted to use a graphical calculator in this paper.

#### **INFORMATION FOR CANDIDATES**

- The number of marks is given in brackets [] at the end of each question or part question.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is 72.
- This document consists of 4 pages. Any blank pages are indicated.

1 20% of packets of a certain kind of cereal contain a free gift. Jane buys one packet a week for 8 weeks. The number of free gifts that Jane receives is denoted by *X*. Assuming that Jane's 8 packets can be regarded as a random sample, find

(i) 
$$P(X = 3)$$
,

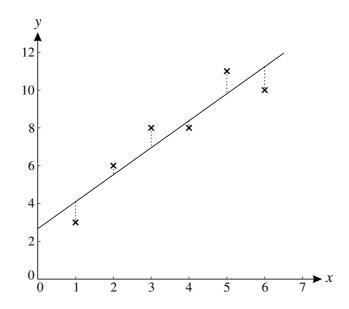
(ii) 
$$P(X \ge 3)$$
, [2]

(iii) 
$$E(X)$$
. [2]

- 2 Two judges placed 7 dancers in rank order. Both judges placed dancers A and B in the first two places, but in opposite orders. The judges agreed about the ranks for all the other 5 dancers. Calculate the value of Spearman's rank correlation coefficient. [4]
- 3 In an agricultural experiment, the relationship between the amount of water supplied, x units, and the yield, y units, was investigated. Six values of x were chosen and for each value of x the corresponding value of y was measured. The results are shown in the table.

х	1	2	3	4	5	6
у	3	6	8	8	11	10

These results, together with the regression line of y on x, are plotted on the graph.



- (i) Give a reason why the regression line of x on y is not suitable in this context. [1]
- (ii) Explain the significance, for the regression line of y on x, of the distances shown by the vertical dotted lines in the diagram. [2]
- (iii) Calculate the value of the product moment correlation coefficient, r. [3]
- (iv) Comment on your value of r in relation to the diagram. [2]

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4	30% of people own a Talk-2 phone. People are selected at random, one at a time, and asked whether
	they own a Talk-2 phone. The number of people questioned, up to and including the first person who
	owns a Talk-2 phone, is denoted by X. Find

(i) 
$$P(X = 4)$$
, [3]

(ii) 
$$P(X > 4)$$
, [2]

(iii) 
$$P(X < 6)$$
.

5 The diameters of 100 pebbles were measured. The measurements rounded to the nearest millimetre, x, are summarised in the table.

X	$10 \leqslant x \leqslant 19$	$20 \leqslant x \leqslant 24$	$25 \leqslant x \leqslant 29$	$30 \leqslant x \leqslant 49$
Number of stones	25	22	29	24

These data are to be presented on a statistical diagram.

- (i) For a histogram, find the frequency density of the  $10 \le x \le 19$  class. [2]
- (ii) For a cumulative frequency graph, state the coordinates of the first two points that should be plotted. [2]
- (iii) Why is it not possible to draw an exact box-and-whisker plot to illustrate the data? [1]
- 6 Last year Eleanor played 11 rounds of golf. Her scores were as follows:

- (i) Calculate the mean of these scores and show that the standard deviation is 5.31, correct to 3 significant figures. [4]
- (ii) Find the median and interquartile range of the scores. [4]

This year, Eleanor also played 11 rounds of golf. The standard deviation of her scores was 4.23, correct to 3 significant figures, and the interquartile range was the same as last year.

(iii) Give a possible reason why the standard deviation of her scores was lower than last year although her interquartile range was unchanged. [1]

In golf, smaller scores mean a better standard of play than larger scores. Ken suggests that since the standard deviation was smaller this year, Eleanor's overall standard has improved.

- (iv) Explain why Ken is wrong. [1]
- (v) State what the smaller standard deviation does show about Eleanor's play. [1]

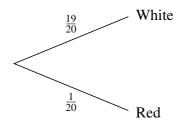
### [Questions 7, 8 and 9 are printed overleaf.]

- 7 Three letters are selected at random from the 8 letters of the word COMPUTER, without regard to order.
  - (i) Find the number of possible selections of 3 letters. [2]
  - (ii) Find the probability that the letter P is included in the selection. [3]

Three letters are now selected at random, one at a time, from the 8 letters of the word COMPUTER, and are placed in order in a line.

- (iii) Find the probability that the 3 letters form the word TOP. [3]
- A game at a charity event uses a bag containing 19 white counters and 1 red counter. To play the game once a player takes counters at random from the bag, one at a time, without replacement. If the red counter is taken, the player wins a prize and the game ends. If not, the game ends when 3 white counters have been taken. Niko plays the game once.
  - (i) (a) Copy and complete the tree diagram showing the probabilities for Niko. [4]

#### First counter



- (b) Find the probability that Niko will win a prize. [3]
- (ii) The number of counters that Niko takes is denoted by X.

(a) Find 
$$P(X = 3)$$
. [2]

- (b) Find E(X).
- **9** Repeated independent trials of a certain experiment are carried out. On each trial the probability of success is 0.12.
  - (i) Find the smallest value of n such that the probability of at least one success in n trials is more than 0.95.
  - (ii) Find the probability that the 3rd success occurs on the 7th trial. [5]



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