

ADVANCED SUBSIDIARY GCE MATHEMATICS (MEI)

4752

Concepts for Advanced Mathematics (C2)

QUESTION PAPER

Candidates answer on the Printed Answer Book

OCR Supplied Materials:

- Printed Answer Book 4752
- MEI Examination Formulae and Tables (MF2)

Other Materials Required:

· Scientific or graphical calculator

Thursday 27 May 2010 Morning

Duration: 1 hour 30 minutes

INSTRUCTIONS TO CANDIDATES

These instructions are the same on the Printed Answer Book and the Question Paper.

- Write your name clearly in capital letters, your Centre Number and Candidate Number in the spaces provided on the Printed Answer Book.
- The questions are on the inserted Question Paper.
- Write your answer to each question in the space provided in the Printed Answer Book. Additional paper
 may be used if necessary but you must clearly show your Candidate Number, Centre Number and question
 number(s).
- Use black ink. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure that you know what you have to do before starting your answer.
- Answer all the questions.
- Do **not** write in the bar codes.
- You are permitted to use a graphical calculator in this paper.
- Final answers should be given to a degree of accuracy appropriate to the context.

INFORMATION FOR CANDIDATES

This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [] at the end of each question or part question on the Question Paper.
- You are advised that an answer may receive no marks unless you show sufficient detail of the working to
 indicate that a correct method is being used.
- The total number of marks for this paper is 72.
- The Printed Answer Book consists of 12 pages. The Question Paper consists of 8 pages. Any blank pages
 are indicated.

INSTRUCTION TO EXAMS OFFICER / INVIGILATOR

Do not send this Question Paper for marking; it should be retained in the centre or destroyed.

Section A (36 marks)

1 You are given that

$$u_1 = 1,$$

$$u_{n+1} = \frac{u_n}{1 + u_n}.$$

Find the values of u_2 , u_3 and u_4 . Give your answers as fractions.

[2]

2 (i) Evaluate
$$\sum_{r=2}^{5} \frac{1}{r-1}$$
. [2]

- (ii) Express the series $2 \times 3 + 3 \times 4 + 4 \times 5 + 5 \times 6 + 6 \times 7$ in the form $\sum_{r=2}^{a} f(r)$ where f(r) and a are to be determined. [2]
- 3 (i) Differentiate $x^3 6x^2 15x + 50$. [2]
 - (ii) Hence find the x-coordinates of the stationary points on the curve $y = x^3 6x^2 15x + 50$. [3]
- 4 In this question, $f(x) = x^2 5x$. Fig. 4 shows a sketch of the graph of y = f(x).

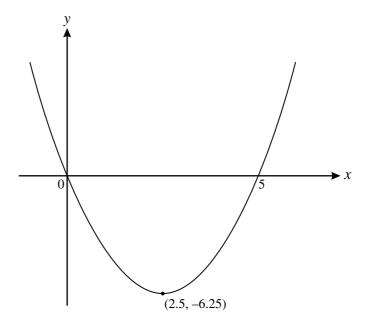


Fig. 4

On separate diagrams, sketch the curves y = f(2x) and y = 3f(x), labelling the coordinates of their intersections with the axes and their turning points. [4]

5 Find
$$\int_{2}^{5} \left(1 - \frac{6}{x^3}\right) dx$$
. [4]

- 6 The gradient of a curve is $6x^2 + 12x^{\frac{1}{2}}$. The curve passes through the point (4, 10). Find the equation of the curve.
- 7 Express $\log_a x^3 + \log_a \sqrt{x}$ in the form $k \log_a x$. [2]
- 8 Showing your method clearly, solve the equation $4 \sin^2 \theta = 3 + \cos^2 \theta$, for values of θ between 0° and 360°.
- **9** The points (2, 6) and (3, 18) lie on the curve $y = ax^n$.

Use logarithms to find the values of a and n, giving your answers correct to 2 decimal places. [5]

Section B (36 marks)

- 10 (i) Find the equation of the tangent to the curve $y = x^4$ at the point where x = 2. Give your answer in the form y = mx + c.
 - (ii) Calculate the gradient of the chord joining the points on the curve $y = x^4$ where x = 2 and x = 2.1.
 - (iii) (A) Expand $(2+h)^4$. [3]

(B) Simplify
$$\frac{(2+h)^4-2^4}{h}$$
. [2]

(C) Show how your result in part (iii) (B) can be used to find the gradient of $y = x^4$ at the point where x = 2.

11 (a)

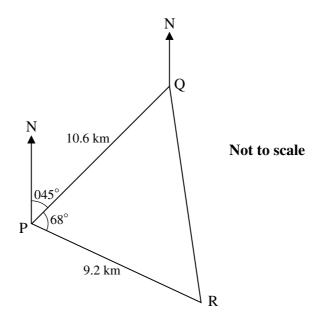


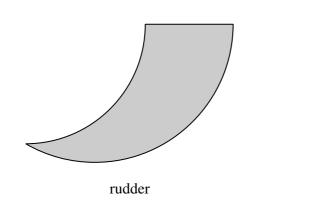
Fig. 11.1

A boat travels from P to Q and then to R. As shown in Fig. 11.1, Q is 10.6 km from P on a bearing of 045°. R is 9.2 km from P on a bearing of 113°, so that angle QPR is 68°.

Calculate the distance and bearing of R from Q.

[5]

(b) Fig. 11.2 shows the cross-section, EBC, of the rudder of a boat.



 $\begin{array}{c|c}
D & A & E & B \\
\hline
 & 2\pi \\
\hline
 & 80 \text{ cm}
\end{array}$

detail of construction

Fig. 11.2

BC is an arc of a circle with centre A and radius 80 cm. Angle CAB = $\frac{2\pi}{3}$ radians.

EC is an arc of a circle with centre D and radius r cm. Angle CDE is a right angle.

(i) Calculate the area of sector ABC.

[2]

(ii) Show that $r = 40\sqrt{3}$ and calculate the area of triangle CDA.

[3]

(iii) Hence calculate the area of cross-section of the rudder.

[3]

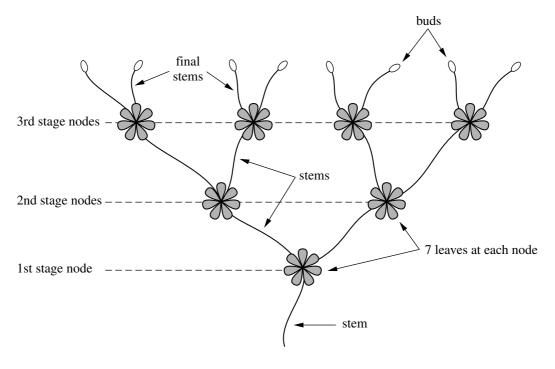


Fig. 12

A branching plant has stems, nodes, leaves and buds.

- There are 7 leaves at each node.
- From each node, 2 new stems grow.
- At the end of each final stem, there is a bud.

Fig. 12 shows one such plant with 3 stages of nodes. It has 15 stems, 7 nodes, 49 leaves and 8 buds.

(i) One of these plants has 10 stages of nodes.

(B) How many stems does it have?

[2]

(ii) (A) Show that the number of leaves on one of these plants with n stages of nodes is

$$7(2^n - 1)$$
. [2]

(B) One of these plants has n stages of nodes and more than 200 000 leaves. Show that n satisfies the inequality $n > \frac{\log_{10} 200\,007 - \log_{10} 7}{\log_{10} 2}$. Hence find the least possible value of n. [4]

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Section A (36 marks)

1	
2 (i)	
2 (ii)	

3 (i)	
3 (ii)	

4	
5	

6	
7	
8	

9	
	Santian P (26 marks)
	Section B (36 marks)
10 (i)	Section B (30 marks)
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10 (i)	Section B (30 marks)
10 (i)	Section B (30 marks)
10 (i)	Section B (30 marks)

10 (ii)	
10 (iii)	
10 (iii) (<i>A</i>), (<i>B</i>) and (<i>C</i>)	

11 (a)	
11 (b) (i)	

11(b)(ii)	
11(b)(iii)	

12(i) (A)	
12(i) (<i>B</i>)	
12 (ii)(A)	

12 (ii)(<i>B</i>)	

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