



Mathematics (MEI)

Advanced GCE

Unit 4777: Numerical Computation

Mark Scheme for June 2013

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations

Annotation in scoris	Meaning
✓and ×	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
۸	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark	Meaning
scheme	
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
сао	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Subject-specific Marking Instructions for GCE Mathematics (MEI) Pure strand

a. Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b. An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

c. The following types of marks are available.

Μ

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

Α

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

В

Mark for a correct result or statement independent of Method marks.

Е

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d. When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e. The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f. Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.



g. Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

h. For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

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Mark Scheme

Question	Answer	Marks	Guidance
1 (i)	$ \begin{array}{c} x_1 - \alpha \approx k(x_0 - \alpha) \\ x_2 - \alpha \approx k(x_1 - \alpha) \end{array} $	M1	Setup
	Subtract and rearrange to $k \approx \frac{x_2 - x_1}{x_1 - x_0}$	M1	Convincing algebra
	Solve first equation for $\alpha \alpha \approx \frac{kx_0 - x_1}{k - 1}$	M1	To given result
		[3]	
1 (11)	Eg $m = 1.5$	B3 [3]	For convincing argument

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	Question		Answer	Marks	Guidance
1	(iii)		(*)		
			0.5		
			0.559616		
			0.609452		
			0.649289		
			0.680028		
			0.703118		
			0.720119	M1	
			0.732454	A1	
			Differences getting smaller so converging, but slowly	E1	
			(**)		
			0.5		
			0.432481		
			0.360717		
			0.289572		
			0.223904		
			0.1673		
			0.121406	M1	
			0.086056	A1	
			Converging to root at zero	E1	
				[6]	

(Question					Answe		Marks	Guid	ance
1	(iv)		(*)							
			0.5		k	α				
			0.559616	0.059616						
			0.609452	0.049837	0.835962	0.863426				
			0.863426							
			0.830793	-0.03263						
			0.809236	-0.02156	0.660625	0.767271				
			0.767271	0.00100						
			0.765889	-0.00138	0 (07717	0 7 () 7				
			0.764925	-0.00096	0.69//1/	0.7627				
			0.7627	2 6E 06				MO		
			0.762697	-3.0E-00 2.5E.06	0 600611	0 762680				
			(*) converge	es more qui	ckly	0.702009		F1		
			(**)	es more qui	CKIY			LI		
			0.7		k	α				
			0.675835	-0.02416						
			0.643783	-0.03205	1.326411	0.774032				
			0.774032							
			0.778995	0.004963						
			0.786187	0.007192	1.449254	0.762986				
			0.762986							
			0.763113	0.000128						
			0.763296	0.000182	1.429871	0.762689				
			0.762689	07 00						
			0.762689	9E-08	1 400256	0 5(2(00		M1		
			0.762689	1.29E-0/	1.429356	0.762689	a final far second			
			(**) conver	ges provide	a a good end	bugn starting	oint is used	EI,EI [0]		
1	(v)		Value is 1 /	182 to 3dp				[2] M1	Т&е	
			v alue 15 1.4	10 Jup				A1	1000	
								A1	Answer	
								[3]		

Q	Juestion	Answer	Marks	Guidance
2	(i)	The data are not evenly spaced so (ordinary) differences will not work	E1	
		Divided differences, however, can accommodate variable spacing	E1	
		Lagrange's method is not well suited to increasing the degree of the approximating	E1	
		polynomial because it requires complete recalculation		
			[3]	
2	(ii)	$\begin{array}{c} 45.00 \\ 35.00 \\ 25.00 \\ 15.00 \\ 5.00 \\ -5.00 \\ 0.0 \end{array} \begin{array}{c} & & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & \\ & & & & \\ & & & \\ & & & & \\ & & & & \\ & & & & \\ &$	G2	
_			[2]	
2	(iii)	x y 1DD 2DD 3DD 4DD 5DD 2.0 1.04 4.0 1.22 0.09000 1.0 1.42 0.07000 0.16000	M1	Re-order values
		$\begin{array}{cccccccccccccccccccccccccccccccccccc$	M1 A1	DD table
		y(2.9) = 1.040 + 0.081 = 1.121 linear + -0.1584 = 0.963 quadratic + 0.347537 = 1.310 cubic + -0.23948 = 1.071 quartic No convergence of estimates, but 4DDs are nearly equal, so quartic a good fit Answer 1.07 (only 2dp in data)	M1A1 M1A1 M1A1 M1A1 E1 E1 A1	
		Answer 1.07 (only 20p in data)	[14]	

Q	uestion		Answer	Marks	Guidance
2	(iv)				
		x y 1DD 2DD	3DD 4DD 5DD		
		4.0 1.22			
		6.0 6.96 2.87000		M1	
		2.0 1.04 1.48000 0.69500		A1	rearrange
		1.0 1.43 -0.39000 0.37400	0.10700		
		0.5 2.23 -1.60000 0.80667	-0.07867 0.05305		
		8.0 40.53 5.10667 0.95810	0.02524 0.05195 -0.00027		
		x = 4.79 gives		M1	T&e
		1.220 + 2.2673	= 3.487 linear	A1	
		+ -0.66435	= 2.823 quadratic	A1	answer
		+ -0.28536	= 2.538 cubic		
		+ -0.53619	= 2.001 quartic		
				[5]	

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Q	uesti	on	Answer									Marks	Guida	ince
3	(i)													
			h	x	У	<i>k</i> 1	. k	2 <i>k</i>	3 k	k 4	new y	M2	setup	
			0.5	0	1	(0.00781	3 0.00781	3 0.06	25 1	1.015625			
			0.5	0.5	1.015625	0.0625	0.21093	8 0.21093	8 ().5	1.25	A2	Result	
			0.5	1	1.25	0.5	0.97656	0.97656	1.68	75 2	2.265625	M1	Exact	
			0.5	1.5	2.265625	1.6875	2.67968	8 2.67968	8	4	5	A1		
			0.5	2	5									
			Cf $v = 1 + 0.2$	$25x^4$ ·	v(2) = 5 s	solution to	$v' = x^3$ is e	exact				E1		
			2	-			<i>.</i>							
			h	x	v	<i>k</i> 1	<i>k</i> 2	<i>k</i> 3	<i>k</i> 4	ne	ew v			
			0.5	0	1	0	0.001953	0.001953	0.03125	1.00	0651	M1	Rerun	
			0.5	0.5	1.00651	0.03125	0.158203	0.158203	0.5	1.200	0521			
			0.5	1	1.200521	0.5	1.220703	1.220703	2.53125	2.519	9531	A1	Result	
			0.5	1.5	2.519531	2.53125	4.689453	4.689453	8	7.401	1042			
			0.5	2	7.401042							B1	Exact	
			Cf $y = 1 + 0.2$	$2x^5$ v	(2) = 7.4	error in so	lution to v'	$= x^4$				E1		
			<i>.</i>		· · ·		<i>.</i>					[11]		

Q	uesti	on					Answer				Marks	Guid	lance
3	(ii)		$ \begin{array}{c} h\\ 0.2\\ 0.2\\ 0.2\\ 0.2\\ 0.2\\ 0.2\\ 0.2\\ 0.2$	x 0 0.2 0.4 0.6 0.8 1 1.2 1.4 1.6 1.8 2	y 1 1.134994 1.193243 1.18463 1.18463 1.10653 1.107613 1.107613 1.175408 1.332919 1.575176 1.848193	k1 0.168294 0.09783 0.020509 -0.03163 -0.04498 -0.02279 0.029779 0.11 0.204615 0.268871 1 1.5	k2 0.136333 0.056918 -0.01171 -0.044 -0.03754 0.001266 0.069232 0.1621 0.251627 0.278311	<i>k</i> 3 0.135593 0.058692 -0.00856 -0.04242 -0.03854 -0.00191 0.063581 0.151587 0.23499 0.272474	<i>k</i> 4 0.097818 0.020444 -0.03164 -0.04474 -0.02226 0.030575 0.111362 0.207694 0.275691 0.267657	new y 1.134994 1.193243 1.18463 1.143096 1.10653 1.107613 1.175408 1.332919 1.575176 1.848193	M3 A3 G2	Setup result graph	
			Local ma 0. 0.0	aximur <i>h</i> 1 1	n, eg x 0.5 1.1 0.46 1.19	y 9552 6441					B1 M1 A1	First Further	
			0.00 0.000 (0.464	1 () 1 ()).464 1.19 4638 1.19)	6451 6451					B1 B1 [13]	answer	

4	77	7
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Question					Ansv	wer				Marks	Guid	lance
4	(i)		pivots in boxes: $ \begin{array}{r} \underline{4} & 3 \\ \underline{2} & 4 \\ \underline{2} & 6 \\ \underline{4} & 1 \\ \underline{2} & 5 \\ \underline{5} \\ $	5 3 2 9	1 4 5 5 35	1 2 3 4 15	solutions 6.5625	$= x_1$	check: 1 2 3 4	M3 A2 A2	Setup 1 st elimination 2 nd elimination	
			4.5	-0.5 4 0.777778 3.777778	4.5 4 1 6 -0.23529	2.5 3 0.111111 4.111111 -0.73529	-3 -3.875 3.125	$= x_2$ $= x_3$ $= x_4$		A1 M2 A2,A2	3 rd elimination Back substitution Solution and check	
			magnitude of determin	nant (produc	t of moduli c	of pivots):	16			M1 A1 [16]	determinant	

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()uesti	on				An	Marks	Guidance				
4	(ii)											
				· ·	_		1 .	solutions	% change	check:	MI	Decrea
			4.01	3	5	1	1	6.533914	-0.43559	1		Re-run
			2	4	3	4	$\frac{2}{2}$			2	AI	
			2	6	2	5	3			3		
			4	2 502741	9	2 501247	4	_		4	M1	% change
				2.303741	0.300234	<i>J.J01247</i> <i>A</i> 501247	2 501247	2	2 44E 12		A1	
				1.00252	4 012460	4.301247	2.301247	-3	2.44E-13			
				-1.99232	4.012409	0.002494	0.110742	-				
					3 79/02	5 9939093	1 100081	-3 86683	-0.21077			
					3.79402	-0 23453	-0 73482	3 133167	0.261357			
						0.23433	0.75402		0.201337			
			magnitude	e of determi	nant (produc	t of moduli	of pivots):	16.07 0.4	4375			
			U		ч		1 /					
								solutions	% change	check:		
			4	3	5	1	1	7.383966	12.51758	1		
			2.01	4	3	4	2			2	M1	Re-run
			2	6	2	5	3			3		
			4	1	9	5	4			4	Α1	% change
				2.4925	0.4875	3.4975	1.4975				111	
				4.5	-0.5	4.5	2.5	-3.3692	12.30661			
				-2	4	4	3					
				г	0.764444	1.005	0.112778	4 050 40	10.0000			
				L	3.777778	6	4.111111	-4.37342	12.86239			
						-0.20912	-0.71912	3.438819	10.04219			
			magnitude	e of determi	nant (produc	t of moduli	of pivots):	14.22 -11	125			
			A small c	hange in <i>a</i> p	roduces sma	ll changes i	n the solution	ons and the d	eterminant		E1	
			A small c	hange in <i>b</i> p	roduces larg	e changes i	n the solutio	ons and the de	eterminant		E1	
		1			C	-					[8]	

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