

# Wednesday 18 May 2016 - Morning

# AS GCE MATHEMATICS

4721/01 Core Mathematics 1

#### **QUESTION PAPER**

Candidates answer on the Printed Answer Book.

#### **OCR** supplied materials:

- Printed Answer Book 4721/01
- List of Formulae (MF1)

Other materials required:

None

**Duration:** 1 hour 30 minutes

## **INSTRUCTIONS TO CANDIDATES**

These instructions are the same on the Printed Answer Book and the Question Paper.

- The Question Paper will be found inside the Printed Answer Book.
- Write your name, centre number and candidate number in the spaces provided on the Printed Answer Book. Please write clearly and in capital letters.
- Write your answer to each question in the space provided in the Printed Answer Book. If additional space is required, you should use the lined page(s) at the end of the Printed Answer Book. The question number(s) must be clearly shown.
- Use black ink. HB pencil may be used for graphs and diagrams only.
- Answer all the questions.
- Read each question carefully. Make sure you know what you have to do before starting your answer.
- Do not write in the bar codes.
- You are **not** permitted to use a calculator in this paper.
- Give non-exact numerical answers correct to 3 significant figures unless a different degree of accuracy is specified in the question or is clearly appropriate.

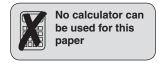
## INFORMATION FOR CANDIDATES

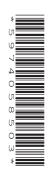
This information is the same on the Printed Answer Book and the Question Paper.

- The number of marks is given in brackets [ ] at the end of each question or part question on the Question Paper.
- You are reminded of the need for clear presentation in your answers.
- The total number of marks for this paper is **72**.
- The Printed Answer Book consists of **12** pages. The Question Paper consists of **4** pages. Any blank pages are indicated.

#### INSTRUCTION TO EXAMS OFFICER/INVIGILATOR

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## Answer all the questions.

- 1 (i) Simplify  $(2x-3)^2 2(3-x)^2$ . [2]
  - (ii) Find the coefficient of  $x^3$  in the expansion of  $(3x^2 3x + 4)(5 2x x^3)$ . [2]
- 2 Express  $\frac{3+\sqrt{20}}{3+\sqrt{5}}$  in the form  $a+b\sqrt{5}$ . [4]
- 3 Solve the simultaneous equations

$$x^2 + y^2 = 34$$
,  $3x - y + 4 = 0$ . [5]

- 4 Solve the equation  $2y^{\frac{1}{2}} 7y^{\frac{1}{4}} + 3 = 0$ . [5]
- 5 Express the following in the form  $2^p$ .

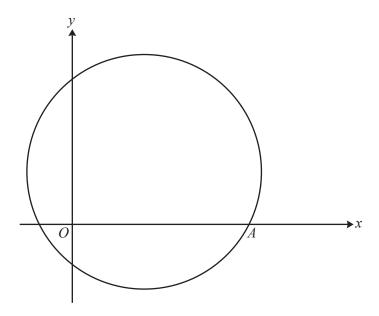
(i) 
$$(2^5 \div 2^7)^3$$

(ii) 
$$5 \times 4^{\frac{2}{3}} + 3 \times 16^{\frac{1}{3}}$$

- 6 (i) Express  $4 + 12x 2x^2$  in the form  $a(x+b)^2 + c$ . [4]
  - (ii) State the coordinates of the maximum point of the curve  $y = 4 + 12x 2x^2$ . [2]
- 7 (i) Sketch the curve  $y = x^2(3-x)$  stating the coordinates of points of intersection with the axes. [3]
  - (ii) The curve  $y = x^2(3-x)$  is translated by 2 units in the positive direction parallel to the x-axis. State the equation of the curve after it has been translated. [2]
  - (iii) Describe fully a transformation that transforms the curve  $y = x^2(3-x)$  to  $y = \frac{1}{2}x^2(3-x)$ . [2]
- 8 A curve has equation  $y = 2x^2$ . The points A and B lie on the curve and have x-coordinates 5 and 5+h respectively, where h > 0.
  - (i) Show that the gradient of the line AB is 20 + 2h.
  - (ii) Explain how the answer to part (i) relates to the gradient of the curve at A. [1]
  - (iii) The normal to the curve at A meets the y-axis at the point C. Find the y-coordinate of C. [3]
- 9 Find the set of values of k for which the equation  $x^2 + 2x + 11 = k(2x 1)$  has two distinct real roots. [7]

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**10** 



The diagram shows the circle with equation  $x^2 + y^2 - 8x - 6y - 20 = 0$ .

(i) Find the centre and radius of the circle.

[3]

The circle crosses the positive x-axis at the point A.

(ii) Find the equation of the tangent to the circle at A.

- [6]
- (iii) A second tangent to the circle is parallel to the tangent at A. Find the equation of this second tangent. [3]
- (iv) Another circle has centre at the origin O and radius r. This circle lies wholly inside the first circle. Find the set of possible values of r.
- 11 The curve  $y = 4x^2 + \frac{a}{x} + 5$  has a stationary point. Find the value of the positive constant a given that the y-coordinate of the stationary point is 32.

# **END OF QUESTION PAPER**

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