

GCE

Mathematics (MEI)

Unit **4754B**: Applications of Advanced Mathematics: Paper B

Advanced GCE

Mark Scheme for June 2017

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.




All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

OCR will not enter into any discussion or correspondence in connection with this mark scheme.

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Annotations and abbreviations

Annotation in scoris	Meaning
 and 	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0 M1	Method mark awarded 0, 1
A0 A1	Accuracy mark awarded 0, 1
B0 B1	Independent mark awarded 0, 1
SC	Special case
	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	Meaning
E1	Mark for explaining
U1	Mark for correct units
G1	Mark for a correct feature on a graph
M1 dep*	Method mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working

Subject-specific Marking Instructions for GCE Mathematics (MEI) Pure strand

- a Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded.

For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

- b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

- c The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, eg by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

E

A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

- d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep *' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.
- e The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

- f Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.
- g Rules for replaced work

If a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests.

If there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others.

NB Follow these maths-specific instructions rather than those in the assessor handbook.

- h For a *genuine* misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question.

Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

Question		Answer	Marks	Guidance
1.	(i)	(All x_0 for which) $0 < x_0 < 1$	B1	Condone as separate inequalities – allow x, x_n , etc. for x_0 Accept (0, 1) (i.e. correct set-notation) – must be strict inequalities
			[1]	
	(ii)	$x_0 = 0$ or 1	B1	Both required - allow x, x_n , etc. for x_0 - condone 0, 1 stated without x_0 (0 and 1 must not appear as part of a range of values)
			[1]	

2.	(i)	$x = 1.6x(1-x)$ $x(1.6x - 0.6) = 0$ $(x = 0 \text{ or } x = \frac{0.6}{1.6} = 0.375 \text{ or } \frac{3}{8})$	<p>M1</p> <p>A1</p>	<p>For correctly replacing x_{n+1} and x_n with x - must be using 1.6</p> <p>Using an iterative approach or stating the correct answer with no working - M0 A0</p> <p>Accept as a minimum the correct equation stated in terms of x only followed by the correct answer for both marks</p>
			[2]	
2.	(ii)	$x^2 - x + 2 = 0$ $\text{Discriminant} = (-1)^2 - 4 \times 1 \times 2 = -7 \text{ or } x = \frac{1 \pm \sqrt{(-1)^2 - 4(1)(2)}}{2}$ <p>so no (real) roots (oe)</p>	<p>M1</p> <p>A1</p>	<p>Re-arranging and correct attempt at either the discriminant or solving using the correct formula/completing the square for their 3-term quadratic equation. Allow consideration of $\sqrt{b^2 - 4ac}$ with correct substitution of their values only</p> <p>Correct working with a correct conclusion (so if discriminant stated must be -7 but may be awarded for $1 - 4(2) \Rightarrow$ no (real) roots/no points of equilibrium)</p> <p>No marks for non-algebraic approach</p>
			[2]	

PLEASE NOTE THAT THE MARKS FOR BOTH 3(i) and 3(ii) MUST BE AWARDED TOGETHER (MAXIMUM OF 6)

3.	(i)	$x_{n+1} = kx_n(1 - x_n) - 0.25$				<p>There may be some variation in the columns for $k = 3$ and $k = 4$. Some calculators will round to the final values earlier than others. In general answers must be given to at least 2dp</p> <p>Allow correct truncated or rounded answers</p> <p>One mark for each column taken far enough</p> <p>B1 $k = 2$ correct to at least x_3</p> <p>B1 $k = 3$ correct to at least x_3 (accept 0.5)</p> <p>B1 $k = 4$ correct to at least x_6 (accept 0.5)</p> <p>B1 $k = 5$ correct to at least x_2</p> <p>isw after reaching the values for each column as stated above</p>	
			$k = 2$	$k = 3$	$k = 4$		$k = 5$
		x_0	0.55	0.55	0.55		0.55
		x_1	0.245	0.4925	0.74		0.9875
		x_2	0.1199...	0.4998...	0.5196		-0.1882...
		x_3	-0.0388...	0.4999...	0.7484...		...
		x_4	...	0.5	0.5030...		...
		x_5	0.7499...		...
		x_6	0.5000...		...
		x_7	0.7499...		...
		x_8	0.5000...		...
		x_9			0.75		
		x_{10}			0.5		
...			

3.	(ii)	<p>For $k = 2$ it is unbounded or ‘dying out’</p> <p>For $k = 3$ it converges (to $x = 0.5$) or stable or equilibrium</p> <p>For $k = 4$ it oscillates (between $x = 0.5$ and $x = 0.75$) or alternates but not fluctuates</p> <p>For $k = 5$, it is unbounded or ‘dying out’</p>	B2	<p>All 4 correct Allow B1 for 2 correct</p> <p>Allow equivalent to ‘dying out’ provided unambiguous</p> <p>Must be one of these three words</p> <p>Must be one of these two words</p> <p>Allow equivalent to ‘dying out’ provided unambiguous</p>
			[6]	

4.	(i)	$3.5644 + \frac{0.0203}{4.6692}$ $= 3.5687$ $3.5687 + 0.0203 \times \left(\frac{1}{4.6692} \right)^2 = 3.5696 \text{ to 5 sf}$	<p>B1</p> <p>B1</p> <p>B1</p>	<p>Correct method - allow a slip in one value (e.g. 4.692) only – either correct value for k implies this mark</p> <p>Accept 3.569 (3.5687476...) – no ft from incorrect values – accept if given as the upper bound of an interval</p> <p>Accept 3.5697 or 3.570 but not 3.57 – no ft from incorrect values – accept if given as an upper bound</p>
			[3]	
4	(ii)(A)	$S = \frac{1}{1 - \frac{1}{4.6692}}$ $S = 1.2725\dots$	<p>M1</p> <p>A1</p>	<p>Use of the correct formula for the sum to infinity of a GP – allow a slip in the value of r only (e.g. 4.692) – allow r stated to 2dp or better ($r = 0.21416945\dots$)</p> <p>Accept 1.273 not 1.27 (1.2725389...)</p> <p>M0 A0 if formula not used</p>
			[2]	
4	(ii)(B)	It is an estimate of a value of k for which chaos is occurring	B1	Accept any mention of ‘chaos’
			[1]	

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