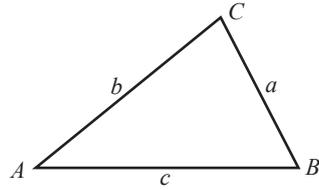


Formulae Sheet: 6993 Additional Mathematics

In any triangle ABC

Cosine rule $a^2 = b^2 + c^2 - 2bc \cos A$



Binomial expansion

When n is a positive integer

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1}b + \binom{n}{2} a^{n-2}b^2 + \dots + \binom{n}{r} a^{n-r}b^r + \dots + b^n$$

where

$$\binom{n}{r} = {}^nC_r = \frac{n!}{r!(n-r)!}$$

Answer **all** the questions.

Section A

- 1 Solve the inequality $2 - x < 1 + 3(x - 2)$. [3]
- 2 The gradient function of a curve is given by $\frac{dy}{dx} = 2 + 2x - 3x^2$.
Find the equation of the curve given that it passes through the point (2, 3). [4]
- 3 The graph of $y = x^2 + 2x - 3$ is given on the grid in the Printed Answer Book.
- (i) Write down the solution to the equation $x^2 + 2x - 3 = 0$. [1]
- (ii) By plotting the appropriate straight line on the grid, find the solution to the equation $x^2 - x - 6 = 0$. [3]
- 4 You are given that the acute angle θ is such that $\sin \theta = \frac{1}{5}$.
Find the **exact** value of each of the following.
- $\cos \theta$
 - $\tan \theta$
- [4]

- 5 Fig. 5 shows part of the graph of the curve with equation $y = 6x^2 - 2x^3$.

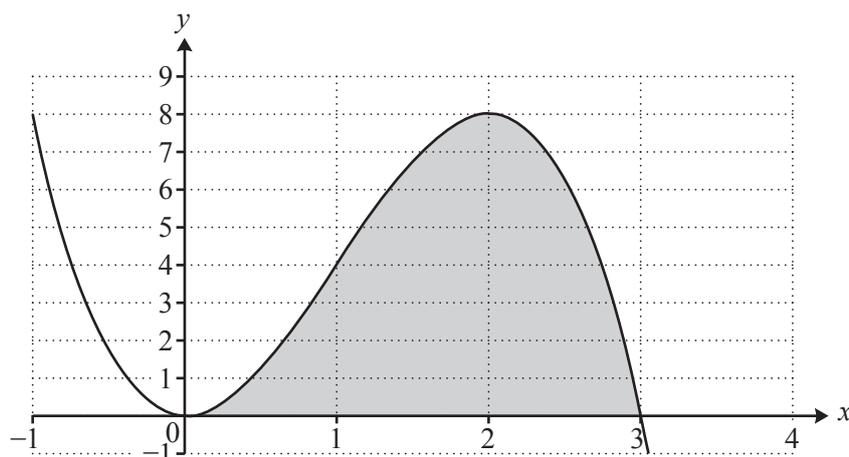


Fig. 5

Find the area of the shaded region enclosed by the curve and the x -axis. [4]

- 6 (i) Solve these simultaneous equations.

$$\begin{aligned} 3x + 4y &= 18 \\ 7x - 3y &= 5 \end{aligned} \quad [4]$$

(ii) Draw a rough sketch of the lines to demonstrate graphically the solution to part (i). [2]

- 7 (i) Find the coordinates of the points where the line $y = 7x - 9$ cuts the curve $y = x^2 + 2x - 5$. [4]

(ii) Determine whether the line is a normal to the curve at either of the points of intersection. [3]

- 8 (i) Simplify the equation $\frac{x+a}{x} + \frac{x-2}{4} = 0$, leaving your answer in the form $(x+p)^2 = q$ where p is an integer and q is given in terms of the constant a . [3]

(ii) Hence write down the range of values of a for which the equation has real roots. [2]

(iii) Using your answer to part (i), solve the equation when $a = -1$, giving your answers **exactly**. [2]

- 9 The proportion of people who are left-handed is 20%.
- (a) For a group of 10 students chosen at random, use the binomial distribution to find the probability that
- (i) no student is left-handed, [2]
- (ii) exactly 4 students are left-handed. [3]
- (b) State the conditions necessary for the binomial distribution to be valid. [2]
- 10 Fig. 10 shows an “up and over” garage door, XY , that is 200 cm long. There is a small wheel at the point G on the door. The wheel runs freely up a groove in a fixed vertical door frame, AB . A metal rod AP is fixed to the top of the door frame, A , and is also fixed to the point P on the door. The rod is hinged at both ends.
- $GP = PX = AP = 60$ cm and $YG = 80$ cm.
- When the door is closed, Y is at B and X is at A . When the door is fully open, G is at A and the door is horizontal, 200 cm above the horizontal ground.

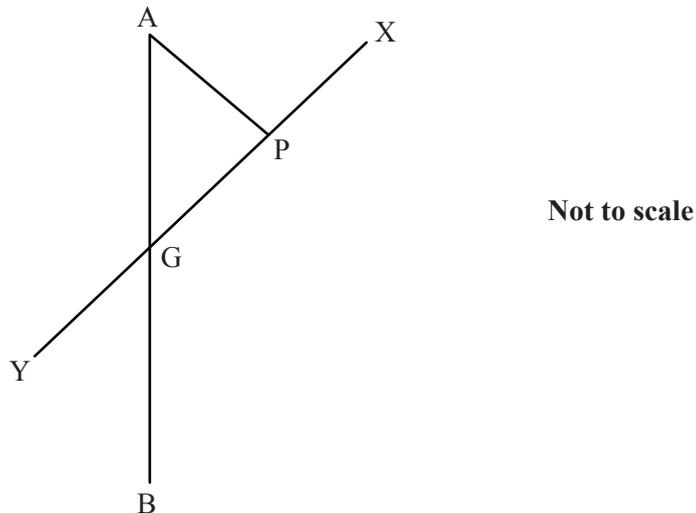


Fig. 10

- (i) Explain why P is the centre of the circle through A , G and X . [1]
- (ii) Hence show that AX is horizontal whatever the position of the garage door. [1]
- (iii) Find the height of Y above the ground when angle $AGP = 40^\circ$. [4]

Section B

11 A circle has centre $(0, 3)$ and radius 3.

(i) Show that the equation of the circle is $x^2 + y^2 - ky = 0$ where k is to be determined. [2]

The line $y = mx - 2$ passes through the point $P(0, -2)$ and is a tangent to the circle.

(ii) Find the two possible values of m . [6]

The two tangents from P meet the circle at the points A and B respectively.

(iii) Find the lengths PA and PB . [4]

12 The shape shown in Fig. 12 is made of metal rods. $ABCD$ is a rectangle.

$AB = CD = y$ cm and $BC = DA = 6x$ cm.

AED is an isosceles triangle with height $4x$ cm and $AE = ED$.

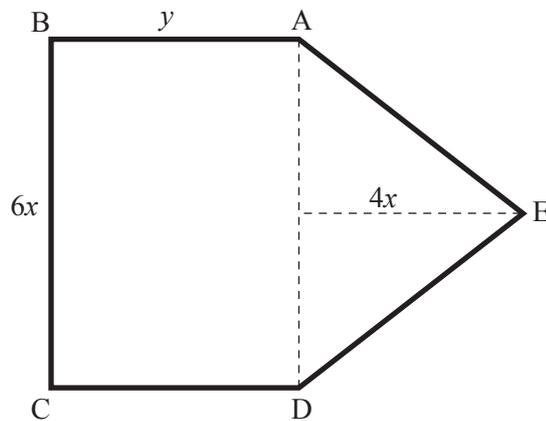


Fig 12

(i) Show that the perimeter, p cm, can be written as $p = 16x + 2y$. [3]

You are given that $p = 96$.

(ii) Show that the area of the shape, A cm², can be written as $A = 288x - 36x^2$. [3]

(iii) Find the maximum area of the shape as x and y vary and find the values of x and y for this area. [6]

- 13 Jessie walks at 3 km per hour in a straight line from a point B to a point C, a distance of 5 km. C is on a bearing 050° from B, as shown in Fig 13.1. Brandon sets out at the same time as Jessie. He starts from a point A which is 2 km due East of B. He walks at 2 km per hour directly to C.

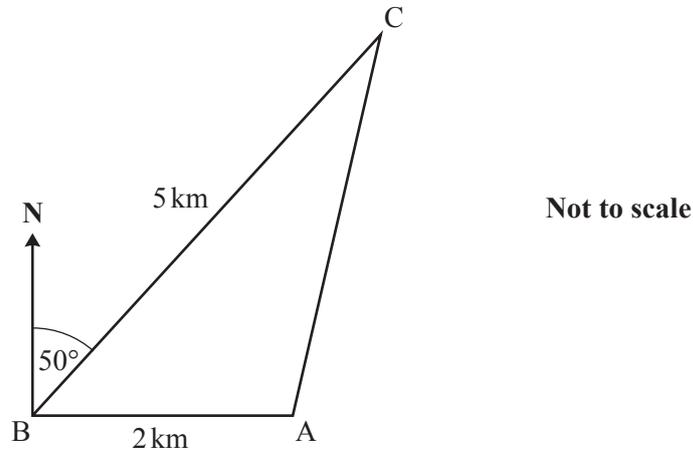


Fig. 13.1

- (i) Calculate the distance AC, correct to 3 significant figures. [4]
- (ii) Show that Brandon arrives at C approximately 11 minutes after Jessie arrives. [3]

Charlie also sets out at the same time as Jessie. He walks in a straight line from A at 2 km per hour to meet Jessie at a point X on BC, as shown in Fig. 13.2. He arrives at the point X at the same time as Jessie.

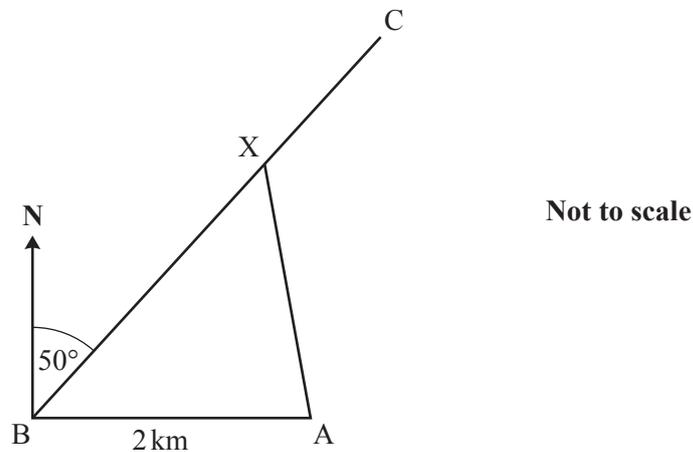


Fig. 13.2

- (iii) Show that there are two possible positions for X and find the bearing on which Charlie must walk in each case. [5]

14 Two cars, P and Q, accelerate from rest from a point O at the same time.

(a) P accelerates uniformly at 2 ms^{-2} .

(i) Write down the formula for the displacement, s metres, of P at time t seconds after leaving O. [1]

(ii) Using appropriate units, find the time taken for P to reach a speed of 90 km h^{-1} . [3]

(b) Q accelerates from rest with **variable** acceleration $a \text{ m s}^{-2}$ where, at time t seconds, $a = 1 + kt$, where k is a positive constant. Q passes P when $t = 10$.

(i) Find the value of k . [5]

(ii) Show that at the time when P reaches 90 km h^{-1} , Q is travelling at a speed just less than 130 km h^{-1} . [3]

END OF QUESTION PAPER

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