

Cambridge Technicals Engineering

Unit 23: Applied mathematics for engineering

Level 3 Cambridge Technical Certificate/Diploma in Engineering
05823 - 05825 & 05873

Mark Scheme for June 2023

OCR (Oxford Cambridge and RSA) is a leading UK awarding body, providing a wide range of qualifications to meet the needs of candidates of all ages and abilities. OCR qualifications include AS/A Levels, Diplomas, GCSEs, Cambridge Nationals, Cambridge Technicals, Functional Skills, Key Skills, Entry Level qualifications, NVQs and vocational qualifications in areas such as IT, business, languages, teaching/training, administration and secretarial skills.

It is also responsible for developing new specifications to meet national requirements and the needs of students and teachers. OCR is a not-for-profit organisation; any surplus made is invested back into the establishment to help towards the development of qualifications and support, which keep pace with the changing needs of today's society.

This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

© OCR 2023

MARKING INSTRUCTIONS

PREPARATION FOR MARKING

RM ASSESSOR

1. Make sure that you have accessed and completed the relevant training packages for on-screen marking: *RM Assessor Assessor Online Training*; *OCR Essential Guide to Marking*.
2. Make sure that you have read and understood the mark scheme and the question paper for this unit. These are posted on the RM Cambridge Assessment Support Portal <http://www.rm.com/support/ca>
3. Log-in to RM Assessor and mark the **required number** of practice responses (“scripts”) and the **number of required** standardisation responses.

YOU MUST MARK 10 PRACTICE AND 10 STANDARDISATION RESPONSES BEFORE YOU CAN BE APPROVED TO MARK LIVE SCRIPTS.

MARKING

1. Mark strictly to the mark scheme.
2. Marks awarded must relate directly to the marking criteria.
3. The schedule of dates is very important. It is essential that you meet the RM Assessor 50% and 100% (traditional 40% Batch 1 and 100% Batch 2) deadlines. If you experience problems, you must contact your Team Leader (Supervisor) without delay.
4. If you are in any doubt about applying the mark scheme, consult your Team Leader by telephone or the RM Assessor messaging system, or by email.
5. **Crossed Out Responses**
Where a candidate has crossed out a response and provided a clear alternative then the crossed out response is not marked. Where no alternative response has been provided, examiners may give candidates the benefit of the doubt and mark the crossed out response where legible.

Multiple Choice Question Responses

When a multiple choice question has only a single, correct response and a candidate provides two responses (even if one of these responses is correct), then no mark should be awarded (as it is not possible to determine which was the first response selected by the candidate).

When a question requires candidates to select more than one option/multiple options, then local marking arrangements need to ensure consistency of approach.

Contradictory Responses

When a candidate provides contradictory responses, then no mark should be awarded, even if one of the answers is correct.

Short Answer Questions (requiring only a list by way of a response, usually worth only **one mark per response**)

Where candidates are required to provide a set number of short answer responses then only the set number of responses should be marked.

The response space should be marked from left to right on each line and then line by line until the required number of responses have been considered. The remaining responses should not then be marked. Examiners will have to apply judgement as to whether a 'second response' on a line is a development of the 'first response', rather than a separate, discrete response. (The underlying assumption is that the candidate is attempting to hedge their bets and therefore getting undue benefit rather than engaging with the question and giving the most relevant/correct responses.)

Short Answer Questions (requiring a more developed response, worth **two or more marks**)

If the candidates are required to provide a description of, say, three items or factors and four items or factors are provided, then mark on a similar basis – that is downwards (as it is unlikely in this situation that a candidate will provide more than one response in each section of the response space.)

Longer Answer Questions (requiring a developed response)

Where candidates have provided two (or more) responses to a medium or high tariff question which only required a single (developed) response and not crossed out the first response, then only the first response should be marked. Examiners will need to apply professional judgement as to whether the second (or a subsequent) response is a 'new start' or simply a poorly expressed continuation of the first response.

6. Always check the pages (and additional lined pages if present) at the end of the response in case any answers have been continued there. If the candidate has continued an answer there then add an annotation to confirm that the work has been seen.
7. Award No Response (NR) if:
 - there is nothing written in the answer space

Award Zero '0' if:














- anything is written in the answer space and is not worthy of credit (this includes text and symbols).

Team Leaders must confirm the correct use of the NR button with their markers before live marking commences and should check this when reviewing scripts.

8. The RM Assessor **comments box** is used by your team leader to explain the marking of the practice responses. Please refer to these comments when checking your practice responses. **Do not use the comments box for any other reason.** If you have any questions or comments for your team leader, use the phone, the RM Assessor messaging system, or e-mail.
9. Assistant Examiners will email a brief report on the performance of candidates to your Team Leader (Supervisor) by the end of the marking period. Your report should contain notes on particular strength displayed as well as common errors or weaknesses. Constructive criticism of the question paper/mark scheme is also appreciated.

10. Annotations (updated for RM assessor marking)

Marking annotations in RM Assessor

Annotation	Meaning
	Correct response
	Incorrect response
	Missing something
	Follow through
	Benefit of doubt
	Ignore subsequent working
	Method mark awarded 0
	Method mark awarded 1
	Accuracy mark awarded 0
	Accuracy mark awarded 1
	Independent mark awarded 0
	Independent mark awarded 1
	Special Case

Mark scheme abbreviations

Other abbreviations in mark scheme	Meaning
oe	Or equivalent
Soi	Seen or implied
www	Without wrong working
ecf	Error carried forward
DM	Method mark dependent on previous M mark

11. Subject specific marking instructions

Annotations should be used whenever appropriate during your marking.

The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. These annotations must be in the body of the work and **not** anywhere near the right-hand margin of each page.

Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct *solutions* leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly.

Correct but unfamiliar or unexpected methods are often signalled by a correct result following an *apparently* incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, award marks according to the spirit of the basic scheme; if you are in any doubt whatsoever (especially if several marks or candidates are involved) you should contact your Team Leader.

The following types of marks are available.

M

A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

DM

A method mark which is dependent on a previous method mark.

A

Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B

Mark for a correct result or statement independent of Method marks.

Unless otherwise indicated, marks once gained cannot subsequently be lost, eg wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

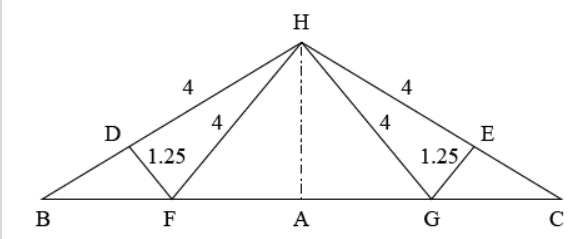
The abbreviation ft implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only — differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, exactly what is acceptable will be detailed in the mark scheme rationale. If this is not the case please consult your Team Leader.

Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise. Candidates are expected to give numerical answers to an appropriate degree of accuracy, with 3 significant figures often being the norm. Small variations in the degree of accuracy to which an answer is given (e.g. 2 or 4 significant figures where 3 is expected) should not normally be penalised, while answers which are grossly over- or under-specified should normally result in the loss of a mark. The situation regarding any particular cases where the accuracy of the answer may be a marking issue should be detailed in the mark scheme rationale. If in doubt, contact your Team Leader.

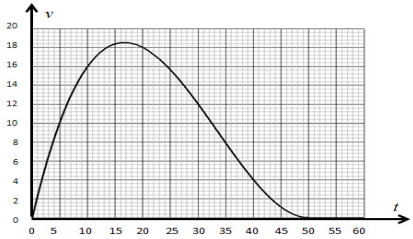
Question		Answer	Marks	Guidance
1	(i)	$(3 - 4 + 3 + 2)\mathbf{i} + (2 + 1 - 3 - 1)\mathbf{j}$ $= 4\mathbf{i} - \mathbf{j}$	M1 A1	Add the four vectors, so i by correct answer. Must be a single vector in component or column vector form SC B1: $i-3j$
			2	
1	(ii)		B1 B1 B1	Point B in correct position (allow without label) At least one of the three direction vectors correct (minimum labelling is an arrowhead) All correct, with labels “B” and “E” Note: Accept with i and j representing vertical and horizontal vectors respectively
			3	
1	(iii)	$\sqrt{(4 - 3)^2 + (-1 - 2)^2}$ $= \sqrt{10} = (3.16\dots)$	M1 A1	Correct Pythagoras for <i>their E</i> from 1i Exact value or 2sf or better
			2	

Question		Answer	Marks	Guidance
2	(i)	<p>[Area =] $A = \frac{1}{2}(a)(a) \sin \theta$</p> $\frac{dA}{d\theta} = \frac{1}{2}a^2 \cos \theta$ $\frac{1}{2}a^2 \cos \theta = 0$ $\theta = 90^\circ$ $h = \frac{a}{\sqrt{2}} \text{ AG}$	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p>	<p>Form an appropriate expression for area using angle θ (or height, but not both)</p> <p>No further Marks without use of calculus</p> <p>Differentiate to obtain appropriate form</p> <p>Correct derivative equated to zero</p> <p>Convincing Pythagoras or trigonometry to obtain correct height</p>
			5	
2	(ii)	$h = \frac{4}{\sqrt{2}} = \frac{4\sqrt{2}}{2} = 2\sqrt{2} = \sqrt{8} = 2.83 \text{ (m)}$	B1	Accept any correct form. 3sf or better, but accept 2.82
			1	
2	(iii)	<p>By recognising that GHE is an isosceles triangle, and using right angled triangle trigonometry</p> $\sin\left(\frac{1}{2}EHG\right) = \frac{\left(\frac{1.25}{2}\right)}{4}$ $E\hat{H}G [= 2 \times \sin^{-1} \frac{0.625}{4} = 17.9785] = 18^\circ$	<p>M1</p> <p>A1</p>	<p>Accept alternatives methods</p> <p>ALT: $\cos EHG = \frac{4^2+4^2-1.25^2}{2 \times 4 \times 4} [= 0.95117]$</p> <p>Note: $\tan^{-1} \frac{0.625}{4} \rightarrow 8.88 \dots \times 2 = 17.761$ is M0,</p> <p>$\tan^{-1} \frac{1.25}{4} = 17.354$ is M0, $\sin^{-1} \frac{1.25}{4} = 18.2099$ is M0</p> <p>$E\hat{H}G = \cos^{-1} 0.95117 = 17.9786 \dots = 18^\circ$</p> <p>Nearest degree, but not from a wrong method</p>
			2	

Question		Answer	Marks	Guidance
2	(iv)	<p>Triangle GHE is isosceles:</p> $H\hat{G}E = \frac{1}{2}(180 - \text{their } 18)$ $= 81(^{\circ})$	<p>M1</p> <p>A1</p>	<p>Any correct alternative method eg cosine rule in triangle GHE, or right angled triangle trigonometry for half of the isosceles triangle GHE, or sine rule in triangle GHE eg $\frac{\sin HGE}{4} = \frac{\sin 18}{1.25}$</p> <p>Note: $\cos^{-1} \frac{1.25}{4}$ is M0, $\tan^{-1} \frac{4}{1.25}$ is M0</p> <p>Nearest degree</p>
			2	
2	(v)	<p>EITHER: Using the right angled triangle HAC to find AC, then doubling</p> $AHC = 45 + \text{their } 18 [= 63^{\circ}]$ $\tan(\text{their } 63) = \frac{AC}{2\sqrt{2}}$ $AC = 2\sqrt{2} \tan(\text{their } 63) [= 5.55]$ $BC = 2 \times AC [= 11.0919] = 11.1 \text{ (m)}$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>Any equivalent method accepted.</p> <p>All method marks available with <i>their</i> answers from 2ii and 2iii</p> <p>Note: $2\sqrt{2} = 2.828$ (<i>their</i> 2ii)</p> <p>AWRT 11.1</p>
		<p>OR: Finding AG and GC, then doubling. Note there are no right angles except at point A</p> $AG = 2\sqrt{2} = 2.283$ $G\hat{E}C = [99] = 180 - \text{their } HEG \text{ 2iii and}$ $E\hat{C}G = [27] = 45 - \text{their } 18 \text{ from 2ii}$ $GC [=2.719] \text{ from sine rule in } \Delta GEC \frac{GC}{\sin 99} = \frac{1.25}{\sin 27}$ $BC = 11.1 \text{ [From } 2 \times (AG + GC)]$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>All method marks available with <i>their</i> answers from 2ii and 2iii</p> <p>soi eg by adding to GC</p> 
			4	

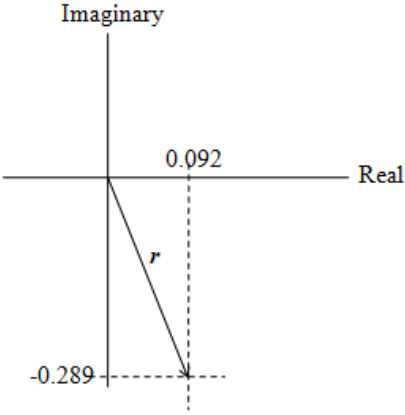
Question		Answer	Marks	Guidance
3	(i)	Evidence of use of moments about fulcrum $3m_1g + 2m_2g = 1.45 \times 10g$ $m_1g + 5m_2g = 1.35 \times 10g$ $3m_1 + 2m_2 = 14.5$ $m_1 + 5m_2 = 13.5$	 M1 M1 A1 A1	Allow without g throughout Note: equations with g substituted are $29.4m_1 + 19.6m_2 = 142.1$ $9.8m_1 + 49m_2 = 132.3$ Two appropriate terms for M1 Two appropriate terms for M1 oe oe
			4	
3	(ii)	$\begin{bmatrix} 3 & 2 \\ 1 & 5 \end{bmatrix} \begin{bmatrix} m_1 \\ m_2 \end{bmatrix} = \begin{bmatrix} 14.5 \\ 13.5 \end{bmatrix}$	 B2FT	FT <i>their</i> equations from (i) All correct B1FT: for any one correct matrix
			2	
3	(iii)	$\text{Det} \begin{bmatrix} 3 & 2 \\ 1 & 5 \end{bmatrix} = 3 \times 5 - 1 \times 2 = 13$ $\begin{bmatrix} 5 & -2 \\ -1 & 3 \end{bmatrix}$ $\begin{bmatrix} m_1 \\ m_2 \end{bmatrix} = \begin{bmatrix} 3 & 2 \\ 1 & 5 \end{bmatrix}^{-1} \begin{bmatrix} 14.5 \\ 13.5 \end{bmatrix} \text{ or } \begin{bmatrix} m_1 \\ m_2 \end{bmatrix} = \frac{1}{13} \begin{bmatrix} 5 & -2 \\ -1 & 3 \end{bmatrix} \begin{bmatrix} 14.5 \\ 13.5 \end{bmatrix}$ $= \frac{1}{13} \begin{bmatrix} 45.5 \\ 26 \end{bmatrix} = \begin{bmatrix} 3.5 \\ 2 \end{bmatrix} \rightarrow m_1 = 3.5 \quad m_2 = 2$	 B1 M1 M1 A1 A1	Non-matrix methods cannot score here Correct determinant soi Forms the adjoint of <i>their</i> matrix Uses $AA^{-1} = I$ to write an appropriate equation Correct equation m_1 and m_2 both correct. Allow in matrix form.
			5	

Question		Answer	Marks	Guidance
4	(i)	$T_H = \ln(2) \times (1000 + 2000) \times 0.00001 = 0.020794\dots$ $T_L = \ln(2) \times 2000 \times 0.00001 = 0.013863\dots$ $T = 0.020794 + 0.013863 = 0.034657\dots$ $f = 1/0.034657 = 28.9\dots \text{ (Hz) or } \frac{20}{\ln 2}$	<p>B1</p> <p>M1</p> <p>A1</p>	<p>One or other correct unsimplified</p> <p>Both attempted and added</p> <p>[28.8539] Answer must round to 28.9</p>
			3	
4	(ii)	$[f =] 0.5 = \frac{1}{1.2 + T_L}$ $T_L = 0.8$ $\ln(2) \cdot R_2 \cdot C = 0.8$ $R_2 = \frac{0.8}{\ln(2) \times 10^{-4}} = 11541.56\dots$ $[T_H =] \ln(2) \times (R_1 + 11541.56) \times 10^{-4} = 1.2$ $R_1 = \frac{1.2}{\ln(2) \times 0.0001} - 11541.56 = 5770.78\dots$ $R_2 \approx 11500 \text{ } (\Omega) \text{ and } R_1 = 5770 \text{ } (\Omega)$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>Substitution and correct process for solving to find R_2</p> <p>Substitution and correct process for solving to find R_1</p> <p>Final A1 for both answers correct and given to 3sf Accept $R_1 = 5810$ (from rounded R_2)</p>
			4	
4	(iii)	$\left[DC = \frac{T_H}{T} \right] = \frac{\ln(2) \times (R_1 + R_2) \times C}{\ln(2) \times (R_1 + R_2) \times C + \ln(2) \times (R_2) \times C} [\times 100]$ $DC = \frac{\ln 2(R_1 + R_2)}{\ln 2(R_1 + R_2 + R_2)} [\times 100] = \frac{R_1 + R_2}{R_1 + 2R_2} \times 100 \text{ AG}$	<p>M1</p> <p>A1</p>	<p>Fraction formed, with all substitutions seen</p> <p>Must show factorisation in the denominator or robust cancellation of terms</p>
			2	
4	(iv)	<p>Minimum [when $R_1 = 0$ and $R_2 > 0$ DC] = 50(%)</p> <p>Maximum [when $R_2 = 0$ and $R_1 > 0$, DC] = 100(%)</p>	<p>B1</p> <p>B1</p>	<p>Sight of 50</p> <p>Sight of 100</p>
			2	

Question	Answer	Marks	Guidance
5 (i)	$v = \int a dt = \int 0.003t^2 - 0.2t + 2.5dt$ $v = \frac{0.003t^3}{3} - \frac{0.2t^2}{2} + 2.5t [+C]$ <p>[Since $v = 0$ when $t = 0$, $C = 0$] $v = 0.001(10^3) - 0.1(10^2) + 2.5(10)$ $v = 16 \text{ (m s}^{-1}\text{)}$</p>	<p>M1 A1</p> <p>M1 A1</p>	<p>Attempt to integrate, with increase in power by one and change of coefficient in at least one term Correct integration (allow without +c)</p> <p>Substitute $t = 10$ into their answer from integration Correct answer without wrong working scores 4/4</p>
5 (ii)	<p>v maximum when $0.003t^2 - 0.2t + 2.5 = 0$</p> $t = \frac{0.2 \pm \sqrt{0.04 - 4 \times 0.003 \times 2.5}}{0.006}$ $t = \frac{50}{3} [16.66..] [and 50..]$ <p>$v(\text{max}) = v(16.7) = 18.5.. \text{ (m s}^{-1}\text{)}$</p>	<p>B1 M1</p> <p>A1</p> <p>A1</p>	<p>soi Attempt to solve a 3 term quadratic, from $a = 0$</p> <p>If $v = 0$ present from speed $t = 50$, then 18.5 must be identified as the maximum speed</p>
5 (iii)		<p>B1</p> <p>B1</p> <p>B1</p>	<p>Maximum at (16.7, 18.5)</p> <p>Starts at (0,0) and finishes at (50, 0)</p> <p>Correct curve shape, with axes labelled</p>
		3	

Question		Answer	Marks	Guidance
5	(iv)	$s = \int_0^{50} 0.001t^3 - 0.1t^2 + 2.5t \, dt$ $s = \left[\frac{0.001t^4}{4} - \frac{0.1t^3}{3} + \frac{2.5t^2}{2} \right]_0^{50}$ $s = 1562.5 - 4166.666\dots + 3125 = 520.833\dots \text{ (m)}$	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>Attempt to integrate, with increase in power by one and change of coefficient in at least one term</p> <p>Correct integration (limits not needed at this stage)</p> <p>Correct use of limits 50 and 0 in their answer from integration soi (allow without sight of $t = 0$)</p> <p>Accept 520 or better</p> <p>Correct answer without wrong working scores 4/4</p>
			4	

Question		Answer	Marks	Guidance
6	(i)	$H(f) = \left[\int_{-\infty}^0 0 e^{-j2\pi ft} dt \right] + \int_0^{\infty} e^{-t} e^{-j2\pi ft} dt$ $\int_0^{\infty} e^{-t(1+j2\pi f)} dt$ $\left[\frac{1}{-(1+j2\pi f)} e^{-t(1+j2\pi f)} \right]_0^{\infty}$ $= \frac{1}{-(1+j2\pi f)} (0 - 1)$ $= \frac{1}{1+j2\pi f} \quad \text{AG}$	<p>B1</p> <p>M1</p> <p>DM1</p> <p>DM1</p> <p>A1</p>	<p>First 3 marks can be scored without limits Sight of correct expression for integral when $t \geq 0$</p> <p>Combine into a single power of e: eg $e^{(-1-j2\pi)t}$</p> <p>Integrate to obtain correct form</p> <p>Correct process using both limits</p> <p>Convincing completion without errors at any stage</p>
			5	
6	(ii)	$\frac{1}{1+j2\pi(0.5)}$ $= \frac{1}{1+\pi j} \times \frac{1-\pi j}{1-\pi j}$ $= \frac{1-\pi j}{1+\pi^2}$ $= \frac{1}{(1+\pi^2)} - \frac{\pi}{(1+\pi^2)} j$ $0.092 + (-0.289)j$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>oe soi</p> <p>Attempt to rationalise by multiplying by conjugate of denominator</p> <p>Obtain single fraction with real denominator</p> <p>Accept 0.092 – 0.289j Final 3 marks implied by correct answer to 3 dp</p>
			4	

Question	Answer	Marks	Guidance
6 (iii)		<p>B1 FT</p>	<p><i>Their</i> H(0.5) plotted on an Argand diagram</p> <p>Values of Re and Im components must be clear</p>
		<p>1</p>	
6 (iv)	<p>$\theta = \tan^{-1}\left(\frac{-0.289}{0.092}\right)$ or $r = \sqrt{0.092^2 + (-0.289)^2}$</p> <p>Both correct 0.303(cos(-1.26) + j sin(-1.26))</p>	<p>M1</p> <p>A1</p>	<p>Correct method for argument or modulus, using <i>their</i> complex H(0.5) from ii</p> <p>Correct to 3sf or better</p>
		<p>2</p>	

Question		Answer	Marks	Guidance
7	(i)	$\left[\frac{5}{30} \times 2\pi\right] = \frac{\pi}{3}$ [rads]	B1	Any equivalent angle in radians. Accept 1.05
			1	
7	(ii)	$\bar{h} = \frac{1}{\pi/3} \int_0^{\pi/3} (4 \cos^2 \theta + 1) d\theta$ $h = 4\left(\frac{1}{2}(\cos(2\theta) + 1) + 1\right)$ $h = 2\cos(2\theta) + 6$ $\bar{h} = \frac{1}{\pi/3} [\sin(2\theta) + 6\theta]_0^{\pi/3}$ $\bar{h} = \frac{3}{\pi} \left(\sin\left(\frac{2\pi}{3}\right) + 2\pi \right)$ $= 6.827 \text{ (m)}$	B1 B1 M1* DM1 A1	Sight of $\frac{1}{\frac{\pi}{3}-0}$ and limits 0 to $\frac{\pi}{3}$. Accept 1.05 Correct unsimplified expression for h in terms of the double angle sin 2θ term from integration Correct limits applied correctly Accept 6.8
			5	
7	(iii)	$E = [4 \times] \frac{1}{2} (11.5 \times 10^6)(1025)(9.8)(5.3^2) \times \frac{10^{-6}}{3600}$ $= 1802.7147 \text{ (MW h)}$	M1 A1	Correct substitutions. Allow without 4 × for M1 Accept 1800
			2	
7	(iv)	<p>Turbines are not 100% efficient [and will produce less energy than the potential energy of the flowing water]</p> <p>During an incoming tide change the lagoon may not fill completely [to a height of h due to restricted water flow through the turbines]</p>	B1 B1	Allow other reasonable explanations eg <ul style="list-style-type: none"> • Calculation assumes there are sufficient numbers of turbines to capture all of the potential energy • Wave power has not been included • Kinetic energy of the moving water is not included <u>Not:</u> <ul style="list-style-type: none"> • The tidal range may vary on the day • Surface area of lagoon may change
			2	

Need to get in touch?

If you ever have any questions about OCR qualifications or services (including administration, logistics and teaching) please feel free to get in touch with our customer support centre.

Call us on

01223 553998

Alternatively, you can email us on

support@ocr.org.uk

For more information visit

 ocr.org.uk/qualifications/resource-finder

 ocr.org.uk

 [Twitter/ocrexams](https://twitter.com/ocrexams)

 [/ocrexams](https://twitter.com/ocrexams)

 [/company/ocr](https://www.linkedin.com/company/ocr)

 [/ocrexams](https://www.youtube.com/ocrexams)



OCR is part of Cambridge University Press & Assessment, a department of the University of Cambridge.

For staff training purposes and as part of our quality assurance programme your call may be recorded or monitored. © OCR 2023 Oxford Cambridge and RSA Examinations is a Company Limited by Guarantee. Registered in England. Registered office The Triangle Building, Shaftesbury Road, Cambridge, CB2 8EA.

Registered company number 3484466. OCR is an exempt charity.

OCR operates academic and vocational qualifications regulated by Ofqual, Qualifications Wales and CCEA as listed in their qualifications registers including A Levels, GCSEs, Cambridge Technicals and Cambridge Nationals.

OCR provides resources to help you deliver our qualifications. These resources do not represent any particular teaching method we expect you to use. We update our resources regularly and aim to make sure content is accurate but please check the OCR website so that you have the most up-to-date version. OCR cannot be held responsible for any errors or omissions in these resources.

Though we make every effort to check our resources, there may be contradictions between published support and the specification, so it is important that you always use information in the latest specification. We indicate any specification changes within the document itself, change the version number and provide a summary of the changes. If you do notice a discrepancy between the specification and a resource, please [contact us](#).

Whether you already offer OCR qualifications, are new to OCR or are thinking about switching, you can request more information using our [Expression of Interest form](#).

Please [get in touch](#) if you want to discuss the accessibility of resources we offer to support you in delivering our qualifications.